

# INVERSE PROBLEMS



In brief

> **Code:** N9EN21

## Presentation

### Objectives

The objectives of this course is to learn and understand various ways to solve inverse problems. Depending on the student's area, applications will be oriented toward photographic 3D-reconstruction methods or numerical problems with uncertainty. In the first case, the problem is to obtain a 3D model of a scene i.e., its shape and its colour. In the second case, the main filtering methods based on the non-linear Bayesian filters (particle filter, Kalman filter, extended Kalman filter, ensemble Kalman filter) will be studied. For a given ODE/SDE, students have to identify the corresponding notion of integration, then should be able to propose an adapted filtering method.

### Description

The content is twofold, with a focus on the student's preferred area:

- Filtering methods

- Introduction to filtering : Bayesian inference ; Filtering and smoothing principles, non-linear filtering ; Application to the linear and Gaussian case: Kalman filter.

- Uncertainty dynamics for ordinary differential equations (ODE) and stochastic differential equations (SDE): from partial differential equation to ODE (numerical schemes); Lyapunov exponent and chaotic system; stochastic processes; discrete/continuous Markov processes; Observable/measure dynamics duality

- Stochastic filtering: Particle filter; Ensemble Kalman filter; Stochastic smoother

---

## Pre-requisites

Optimization, notion of probability and statistics, numerical linear algebra

## Useful info

---

### Place

› Toulouse